



Free-Space Quantum Key Distribution by Rotation-Invariant Twisted Photons

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“Twisted photons” are photons carrying a well-defined nonzero value of orbital angular momentum (OAM). The associated optical wave exhibits a helical shape of the wavefront (hence the name) and an optical vortex at the beam axis. The OAM of light is attracting a growing interest for its potential in photonic applications ranging from particle manipulation, microscopy, and nanotechnologies to fundamental tests of quantum mechanics, classical data multiplexing, and quantum communication. Hitherto, however, all results obtained with optical OAM were limited to laboratory scale. Here, we report the experimental demonstration of a link for free-space quantum communication with OAM operating over a distance of 210 m. Our method exploits OAM in combination with optical polarization to encode the information in rotation-invariant photonic states, so as to guarantee full independence of the communication from the local reference frames of the transmitting and receiving units. In particular, we implement quantum key distribution, a protocol exploiting the features of quantum mechanics to guarantee unconditional security in cryptographic communication, demonstrating error-rate performances that are fully compatible with real-world application requirements. Our results extend previous achievements of OAM-based quantum communication by over 2 orders of magnitude in the link scale, providing an important step forward in achieving the vision of a worldwide quantum network.

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Introduction.—Quantum key distribution (QKD) has taken its initial steps out of the laboratory years ago and is nowadays included in commercial devices that use optical fiber (wire-line) systems. With state-of-the-art technology, QKD on a regional scale has been already demonstrated in the U.S.A., Europe, China, Canada, and Japan. However, free-space optical links are required for long-distance communication among areas which are not suitable for fiber installation or for moving terminals, including the important case of satellite-based links. Among the various implementation schemes proposed so far, the protocol reported by D'Ambrosio *et al.* [1] is unique in its exploitation of spatial transverse modes of the optical beam, in particular, of the orbital angular momentum (OAM) degree of freedom, in order to acquire a significant technical advantage that is the insensitivity of the communication to the relative alignment of the users' reference frames. This advantage may be very relevant for the QKD implementations to be upgraded from the regional scale to a national or continental one, or for links crossing hostile ground, and even for envisaging a QKD on a global scale by exploiting orbiting terminals on a network of satellites.

In the last decades, the OAM of light has been widely investigated as a new promising resource both for fundamental and applied physics. Indeed, properties of OAM have been exploited for applications in many different

fields, such as microscopy [2], astronomy [3,4], metrology [5], fundamental quantum mechanics [6], and biophysics [7]. This degree of freedom of light can be used to specify the azimuthal dependence of the transverse modes of the electromagnetic radiation. The OAM eigenmodes are characterized by a twisted wavefront composed of ℓ intertwined helices, where ℓ is an integer, and by photons carrying $\ell\hbar$ of (orbital) angular momentum, in addition to the more usual spin angular momentum associated with polarization. The potentially unlimited value of ℓ opens the possibility to exploit OAM also for increasing the capacity of communication systems (although at the expense of increasing also the channel cross-section size), and classical data transmission based on OAM multiplexing has been recently demonstrated both in free space [8–10] and optical fibers [11]. Such a feature can also be exploited in the quantum domain, for example, to expand the number of qubits per photon [12–14], or to achieve new functions, such as the rotational invariance of the photonic qubits, as in the present work.

OAM is a conserved quantity for light propagation in vacuum, which is obviously important for communication applications. However, OAM is also highly sensitive to atmospheric turbulence, a feature which limits its potential usefulness in many practical cases. Several theoretical studies have been devoted to the investigation of turbulence effects on the OAM propagations in free space [15–18].

Experiments were performed by simulating the effects of the atmospheric turbulence by adding random phase fluctuations [19] or by using turbulence cells [20]. An experiment of classical communication with the free-space propagation of OAM was performed with radio waves (at a wavelength $\lambda = 12.5$ cm) at a propagation distance of $d = 442$ m (corresponding to about 3500 wavelengths), in which OAM states were used as a multiplexing resource for classical communication [21]. In the optical domain, free-space classical communication of OAM has been demonstrated in Ref. [8]. None of these experiments involved quantum communication. To our knowledge, no free-space propagation of OAM-carrying photons in a quantum regime across distances greater than a few meters has been demonstrated up to now. In the present Letter, we report the realization of free-space alignment-free QKD across air for a distance $d = 210$ m (corresponding to $\sim 2.5 \times 10^8$ wavelengths) exploiting OAM in combination with polarization to encode the quantum bits. As compared with the standard polarization-only encoding, our protocol with OAM has the advantage of being frame independent, thus removing the need for precise alignment of the transmitting and receiving unit frames (although, of course, not the need for accurate beam pointing). On the other hand, compared to OAM only, the polarization component in our communication scheme guarantees a high robustness against spatial perturbations.

Experiment.—In a general bipartite free-space QKD scenario, two users (usually called Alice and Bob) must establish a shared reference frame (SRF) in order to communicate with good fidelity. Indeed, the lack of a SRF is equivalent to an unknown relative rotation which introduces noise into the quantum channel, disrupting the communication. When the information is encoded in photon polarization, such a reference frame can be defined by the orientations of Alice’s and Bob’s “horizontal” linear polarization directions. The alignment of these directions needs extra resources and can impose serious obstacles in long-distance free-space QKD and/or when the misalignment varies in time [22,23]. As already mentioned, a possible solution to this problem can be achieved by using rotation-invariant photonic states, which remove altogether the need for establishing a SRF [1]. Such states are obtained as a particular combination of OAM and polarization modes (hybrid states), for which the transformation induced by the misalignment on polarization is exactly balanced by the effect of the same misalignment on spatial modes. More in detail, although circular polarization states are eigenstates of a reference frame rotation operator, they acquire different phase shifts, causing a rotation of linear polarization states. The adoption of hybrid qubits exactly compensates these phase shifts for both circular polarizations, hence resulting in rotational-invariant photon states [1,24]. Moreover, this rotation-invariant hybrid space can also be regarded as a particular decoherence-free

subspace of the four-dimensional OAM-polarization product Hilbert space, insensitive to the decoherence associated with random rotations.

The hybrid states used in our experiment can be generated by a particular space-variant birefringent plate having topological charge q at its center, named the “ q -plate” [25–27]. In particular, a polarized Gaussian beam (having zero OAM) passing through a q -plate with $q = 1/2$ will undergo the following transformation:

$$(\alpha|R\rangle + \beta|L\rangle)_\pi \otimes |0\rangle_O \rightarrow \alpha|L\rangle_\pi \otimes |r\rangle_O + \beta|R\rangle_\pi \otimes |l\rangle_O. \quad (1)$$

In the previous expression, $|L\rangle_\pi$ and $|R\rangle_\pi$ denote the left and right circular polarization states (eigenstates of spin angular momentum with eigenvalues $+\hbar$ and $-\hbar$, respectively), $|0\rangle_O$ represents the transverse Gaussian mode (with zero OAM and $|l\rangle_O$ and $|r\rangle_O$ the eigenstates of OAM with $|l| = 1$ and with eigenvalues $+\hbar$ and $-\hbar$, respectively), and the subscripts π and O stand, respectively, for polarization and orbital angular momentum. The states appearing on the right-hand side of Eq. (1) are rotation-invariant states [1]. The reverse operation to Eq. (1) can be realized by a second q -plate with the same q . In practice, the q -plate operates as an interface between the polarization space and the hybrid one, converting qubits from one space to the other and vice versa in a universal (qubit-invariant) way. This, in turn, means that the initial encoding and final decoding of information in our QKD implementation protocol can be conveniently performed in the polarization space, while the transmission is done in the rotation-invariant hybrid space.

Let us now describe the alignment-free free-space QKD experiment. We implemented the so-called Bennett-Brassard 1984 protocol [28] with decoy states [29,30]. The bits are encoded in two mutually unbiased bases $\mathbb{Z} = \{|0\rangle, |1\rangle\}$ and $\mathbb{X} = \{|+\rangle, |-\rangle\}$, where $|0\rangle$ and $|1\rangle$ are two orthogonal states spanning the qubit space and $|\pm\rangle = \frac{1}{\sqrt{2}}(|0\rangle \pm |1\rangle)$. Alice randomly chooses between the \mathbb{Z} and \mathbb{X} bases to send the classical bits 0 and 1. In our hybrid encoding, the \mathbb{Z} basis states correspond to $\{|L\rangle_\pi \otimes |r\rangle_O, |R\rangle_\pi \otimes |l\rangle_O\}$, while the \mathbb{X} basis states correspond to $\frac{1}{\sqrt{2}}(|L\rangle_\pi \otimes |r\rangle_O \pm |R\rangle_\pi \otimes |l\rangle_O)$. The transmitter uses four different polarized attenuated lasers to generate the quantum bits. Photons were delivered via a single-mode fiber to a telescope. Polarization states $|H\rangle$, $|V\rangle$, $|R\rangle$, and $|L\rangle$ (as defined in the transmitter reference frame) are then transformed into rotation-invariant hybrid states by means of a q -plate with $q = 1/2$ (see Fig. 1). The photons are then transmitted to the receiving station, where a second q -plate transforms them back into the original polarization states $|H\rangle$, $|V\rangle$, $|R\rangle$, and $|L\rangle$, as defined in the receiver reference frame. Qubits are then analyzed by polarizers and single-photon detectors. The sifted key is obtained by keeping only the bits corresponding to the same basis at the

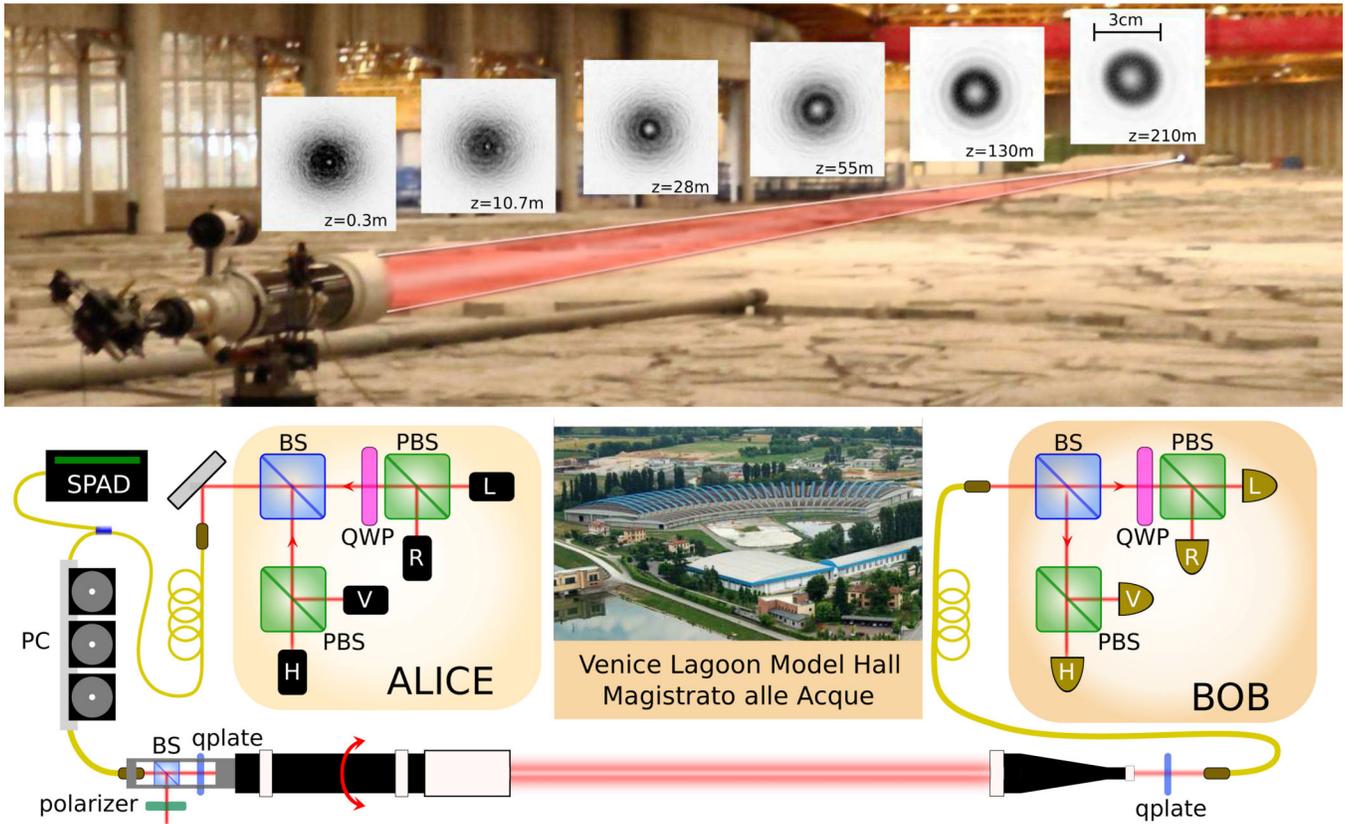


FIG. 1 (color online). Experimental setup. Top image: The experimental layout inside the Venice Lagoon Model Hall located in Padua. Alice's telescope is on the left, and Bob's is the one on the far right. The beam profile versus propagation distance z from the telescope is shown in square frames, all having the same side length of 60 mm. Bottom image: Alice's and Bob's setups. L , R , V , and H are four attenuated lasers that generate the polarization qubits, calibrated by using a SPAD. Before starting the QKD, a PC is used to impose the correct transfer of the polarization states to the telescope by an optical fiber. On the telescope front focal plane, the polarization qubits are transformed by the q -plate into hybrid polarization-OAM qubits and sent toward the receiver. At Bob's terminal, the beam is gathered by a $15\times$ beam compressor and sent to the second q -plate. Here, the hybrid polarization-OAM qubits are transformed back into polarization ones, which are then coupled into a single-mode fiber for spatial-mode filtering and transferred to the Bennett-Brassard 1984 protocol state analyzer.

Alice and Bob sides. The measured transmission of the channel is $\eta_{\text{ch}} \sim 10\%$ (it includes all the losses in the receiving optics before coupling into a single-mode fiber), while the coupling efficiency into a single-mode fiber is given by $\eta_c \sim 25\%–35\%$.

To experimentally demonstrate that our apparatus is insensitive to the relative reference frames of the users, we performed different QKD experiments by rotating the first telescope around the link axis by the following angles: $\theta = 15^\circ$, 45° , and 60° . After each rotation, at Alice's side, we compensated the possible polarization alterations arising from the fiber torsion within the transmitting unit and reoptimized the beam pointing. No compensation was performed at Bob's terminal.

The experiment was performed at the Experimental Center for Hydraulic Models of the "Magistrato alle Acque di Venezia," inside the Venice Lagoon Model Hall (see the inset of Fig. 1). This allows us the demonstration of the polarization-OAM encoding and its decoding by

single-mode fiber coupling in a free-space channel. The location was chosen in order to study a substantial free-space propagation in reproducible environmental conditions. The effect of the turbulence on secure key generation is analyzed in the Supplemental Material [31]. Alice's setup is based on four attenuated lasers (with wavelengths of 850 nm) with four different polarizations: horizontal H , vertical V , left handed L , and right handed R [L and R are obtained by the combination of the laser's polarization and a quarter-wave plate (QWP)]. Qubits are sent in blocks of 2880 bits. A field programmable gate array (FPGA) based controller drives the four lasers at a frequency of 2.5 MHz. In our experimental realization, due to constraints with FPGA data communication, the sending rate resulted in about 30 kbit/s. Photons are coupled into a single-mode fiber, and a fiber beam splitter delivers 95% of the signal to the transmitter telescope and 5% to a single-photon detector (SPAD) used to estimate the mean photon number per pulse. In the telescope cage, a beam splitter (BS) delivers half of the photons to a polarizer

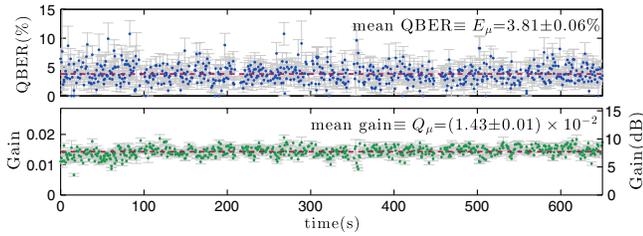


FIG. 2 (color online). Experimental QBER and gain. We show the experimental QBER and gain of the signal state μ (and their statistical errors) at zero rotation angle for each block of 2880 raw bit data. The data show 10 min of acquisition. Dashed lines represent mean values $E_\mu = 3.81\%$ and $Q_\mu = 1.41 \times 10^{-2}$ used for the key-rate evaluation, while 0.06% and 0.01×10^{-2} represent the errors on the mean values. QBER and gain fluctuations from block to block are due to transmission fluctuation caused by the channel turbulence and to the finite size of the blocks.

and the other half to a q -plate with topological charge $q = 1/2$. The polarizer, together with the polarization controller (PC), allows Alice to correct the fiber-induced polarization rotations. The q -plate maps polarization-encoded qubits into qubits encoded in hybrid polarization-OAM states. After the q -plate, the photons enter a 12 cm aperture telescope with focal length $f = 900$ mm ($12 \times$ magnification) and are sent toward the receiving station. The magnification was chosen in order to have a nearly collimated beam between the transmitter and the receiver. We used a telescope aperture large compared to the beam diameter in order to minimize the diffraction effects due to beam clipping. The telescope is mounted on a rotation stage, allowing the rigid rotation of the entire transmitter device. At Bob's receiving station, a 5 cm aperture telescope collects the photons (with losses due to beam clipping of the order of 2%), and a second q -plate decodes the hybrid polarization-OAM qubit states into polarization qubits. The photons are then coupled into a single-mode fiber and delivered to the measurement device, consisting of a beam splitter (BS), a QWP and two polarizing beam splitters (PBS). The four different single-photon detectors are associated with the four polarization states H , V , R , and L .

Secret key-rate analysis.—After the sifting phase, the receiver and the transmitter have two correlated bit sequences: we then measured the quantum bit error rate (QBER) defined as the ratio of the number of errors over the received bits. In Fig. 2, we show 10 min of transmission: in particular, we report the QBER and the gain of the signal states for the angle $\theta = 0$. The gain is the ratio of detected bits over the sent bits. It is possible to see that the transmission is stable over several minutes. Next, we report the QBER of the protocol for different angles. It is important to notice that, if polarization states were used instead of the hybrid rotation-invariant states, the QBER would depend on the relative angle θ between Alice's and Bob's reference frames as $\text{QBER} = \frac{1}{2} \sin^2 \theta$ (the circular states $|R\rangle$ and $|L\rangle$ are rotationally invariant, while the linear polarization states will

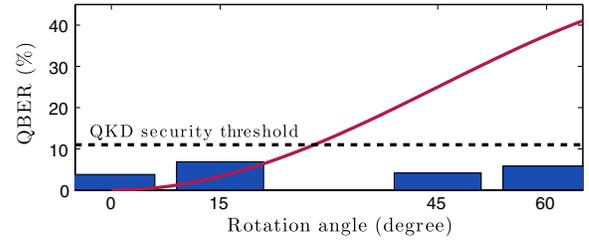


FIG. 3 (color online). Mean QBER. We show the QBERs obtained for the signal state μ at four different rotation angles of the transmitter device 0° , 15° , 45° , and 60° . The mean QBERs are evaluated over 10^5 sifted bits, and their statistical errors are below 0.1%. The dashed line represents the upper limit of the QBER allowing a positive key rate in the infinite key limit with true single-photon sources, namely, 11%. The continuous red line represents the theoretical QBER that would be obtained by standard polarization encoding, using the polarization states $|H\rangle$, $|V\rangle$, $|L\rangle$, and $|R\rangle$.

introduce an error of $\sin^2 \theta$). In Fig. 3, we show the experimental mean QBER obtained at different angles and compare it with the theoretical QBER that would be obtained with polarization encoding. It is evident that, as expected, the angle of rotation does not change the QBER: the observed variations in the measured QBER are ascribed mainly to imperfections in Alice's local polarization compensation.

Finally, we extracted a secret key between the two users, by using the so-called decoy state method [29,30], avoiding a photon number splitting attack on the QKD protocol. We obtained secret keys according to the secret key rate (defined as the number of secure over sifted bits) in the infinite key-length limit given by

$$r = \frac{Q_1^L}{Q_\mu} [1 - h_2(e_1^U)] - \text{leak}_{\text{EC}} + \frac{Q_0}{Q_\mu}. \quad (2)$$

The term leak_{EC} represents the fraction of revealed bits during the performed classical error correction based on the cascade protocol, whose efficiency, given by $f(E_\mu) = \frac{\text{leak}_{\text{EC}}}{h_2(E_\mu)}$, is below 1.05. See the Supplemental Material for the definition and the values measured for different rotation angles of the different terms appearing in the previous equation [31].

In Fig. 4, we show the achieved secret key rates for different angles. We also compare the rates obtained

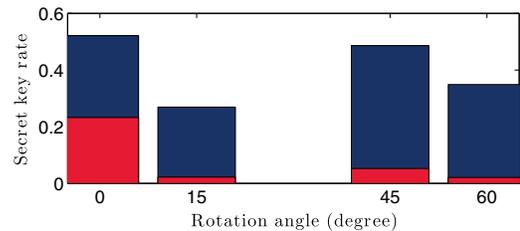


FIG. 4 (color online). Secret key rates at different angles. Secret key rates obtained with the decoy state method (red bars or light gray) and corresponding key rates achievable with true single-photon sources (blue bars or dark gray).

with the decoy state method with the optimal rates that could be achieved with communication performed at the same QBER but using a true single-photon source at the transmitter. In this case, the achievable key rate becomes $r = 1 - h_2(E_\mu) - \text{leak}_{\text{EC}}$.

Conclusions.—In summary, we have demonstrated free-space QKD across 210 m without need for aligning the reference frames of the transmitting and receiving units. This was achieved by using rotation-invariant photonic states obtained as specific polarization-OAM combinations. The demonstrated method is, in principle, not limited to QKD but could be extended to full quantum communication of arbitrary qubits. Our experiment also provides a new record of distance for free-space quantum communication with OAM states, extending previous achievements by more than 2 orders of magnitude. The extension of the present results to a larger Hilbert space is left for future research programs.

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Note added.—Recently, classical communication of different OAM states has been reported in Ref. [34].

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